# Top Fuel Dragster Performance Simulation

The Simulation can be run or modified with Mathcad 14/15. Free Trial at: http://www.ptc.com/product/mathcad/free-trial
<a href="http://www.leapCad.com/TopDragsterPerformanceSimulation.xmcd">Mathcad Simulation at: http://www.leapCad.com/TopDragsterPerformanceSimulation.xmcd</a>
9-19-2015



# **Goal: Simulate Top Fuel Dragster Performance**

## **TABLE OF CONTENTS**

- I. Introduction Basics
- **II.** Macro Model Performance Discussion:
- **III. Specifications & Engineering Estimates: Peak Acceleration**
- IV. Tire Traction & Control Models: Perfect Tire Grip, Tires  $\mu = 4$
- V. Model Results & Validation Validates that Simulation Results Match Data
- VI. Performance Curves of Model Results
- VII. Tire Friction/Grip (Tire Composition and Width)

## **I.** Introduction - Basics

#### Examining the 2010 Kalitta Motorsports Dragster Specs (2014 has 1.25X Power & Torque) <u>Specifications March 13, 2010</u> http://www.popularmechanics.com/cars/a12596/anatomy-of-a-top-fuel-dragster/

Max hp: 8,000 hp(2014 Specs 10,000 hp) 1.25XTorque: 8100 N-M, 6000 lbf ft(2014 Specs 7400 ft lbf) 1.23X90% nitromethane 10% alchohol, 5 gal/4 sec, with 700 hp superchargerClutch is Critical: 5 disc clutch - no transmission. Controlled by centrepital force.Gear Ratio: 3.20 to 1Goodyear large diameter, large width, low inflation pressure tire.R36x17.5-16"36" diameter at start, expand to 44 in, average 40 inTrack coated with adhesive for maximum traction.Tire Coefficient of Friction: 4Front wheels are off the ground for first 200 ft of run						
Magnetos 44 amps per spark plug <b>Performance Table: sec, ft, mp</b>						
Weight	2300 lbf					
Perfor	<u>mance Specs, Perf Table</u>	0.5	10.27	73.80		
0.5 s		0.5	10.27	15.07		
1 sec	52 ft 113.82 mph	1	52	113.82		
1.5s	125 ft 162 mph	1.5	125	162		
	232 ft 213 mph 7 7200 rpm PerfTab :	= 2	X         harger         centrepital force.         erage 40 in         5       0         5       0         5       10.27         5       125         125       162         232       213         5       379.9         248.5			
	379.9 ft 248.5 mph 6599 rpm					
	566 ft 271.6 mph	2.5	379.9	248.5		
3.83 s	1000 ft 321.6 mph	3	566	271.6		
		3.83				

## II. Macro Performance Model Discussion & Description of the Model

**Macro Model:** Macro Models requires only limited knowledge of internal parameters. We treat the system as a Black Box. That is, we don't know the details of what's inside, just a few fundamental parameters. We are only interested in overall performance. Ignore the intricacies. Simple, but not too simple. May not know what is inside, but regardless, the laws of Physics still apply. **This model ignores the initial boost in acceleration from aerodynamic down forces and the 700 hp Power Losses needed to operate the SuperCharger. It does include aerodynamic and tire drag forces.** We will just use the basic physical parameters such as given in Section III and Section IV Models:

### Read Data Plot Data for Power and Torque vs. RPM 2009 Castillo

PowerPlot := READPRN("Castillo Top Drag RPM vs Power.csv") - 12	rows(PowerPlot) = 56
TorquePlot := READPRN("Castillo Top Drag RPM vs Torque.csv")	rows(TorquePlot) = 54

f := 30

### **Fit Power Curves to Data Plots**

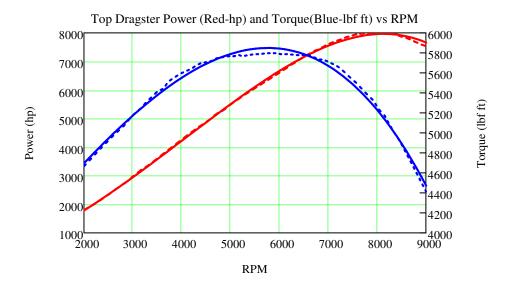
Guess	a := 1	b := 1	<u>c</u> .≔ 1	d := 27	e.:= 1
			spd :=		$\langle 0 \rangle$
Torq –	$a \cdot (spd)^3 - 1$	$b \cdot (spd - c)^2$	$-d \cdot (spd - d)$	e) + f = 0	
Torque(	$(s) := At_0 \cdot (s)$	$a^3 - At_1 \cdot (s + s)$	$-At_2^2 - At_2$	$x_3 \cdot (s - At_4)$	+ At <sub>5</sub>

At := Minerr(a, b, c, d, e, f) Torque(6000) = 5844.32  $S_{m}$  := 2000, 2100.. 9000 Torque<sub>max</sub> := max(Torq) = 5799.13

### Calculate Power as Torque x RPM

 $Power(RPM) := Torque(RPM) \cdot \frac{RPM \cdot lbf \cdot ft \cdot 2 \cdot \pi}{60 \cdot s}$ 

d (ft)	0	60	330	660	1000	1320
t (s)	0	0.842	2.142	3.058	3.831	4.500
v (mph)	-	-	-	280.66	-	334.15



# **III. Specifications & Engineering Estimates: Peak Acceleration**

Max Power:	$Power_{max} := 8000 \cdot hp$	RPM <sub>max</sub> := 9000	Gear Ratio:	GR := 3.20		
<u>Max Torque</u>	$T_{max} := Torque_{max} \cdot lbf \cdot ft$	Rear Tire: R36x17.5-16"	$r_{tire} := \frac{40}{2} in$	$F_{\text{Motor}_{\text{Max}}} := \frac{T_{\text{max}} \cdot GR}{T_{\text{max}} \cdot GR}$		
Tire Coefficient of Friction, µ:	$T_{max} = 5799.13  \text{lbf} \cdot \text{ft}$ $\mu := 4$	$\operatorname{car}_{\max_g} := \mu \cdot g$	k := 1000	$\tau := 1 \cdot \sec$		
Curb Weight:	$M_{curb} := 23001bm$	$M_{gross} := M_{curb} + 160lbm =$	2460·1bm			
Aerodynamic Drag Coeff (TM):	Cd := 0.35	Average Wind Velocity:	$Vw := 0 \cdot mph$			
Cross Wind Drag Coff:	$Cd_{cw} := 0.000014$	Effective Cross Wind V:	$V_{cw} := 0 \cdot mph$			
Shape Correction Factor:	SCF := 0.85	Vehicle Frontal Dimensions:	Af := $(57 - 7.9)$	in·77·in		
Air Density, tire resistance:	$\rho := 1.293 \cdot \frac{\text{gm}}{\text{liter}}$	Drag Frontal Area	$Ad := Af \cdot SCF$	$Ad = 2.07 \cdot m^2$		
Road Rolling Resistance:	$RR_{road} := 0.007$	Tire Rolling Resist, Hys:	$RR_{tire} := 0.011$	$T_{hys} := 0 \cdot \frac{sec}{m}$		
Effective Mass Coefficient:	k <sub>m</sub> := 1.0447	$g_{max} \coloneqq \frac{T_{max} \cdot GR}{M_{gross} \cdot k_m \cdot r_{tire} \cdot g}$	g <sub>max</sub> = 4.33	$\operatorname{RPM}_{\operatorname{motor}} \coloneqq \frac{\operatorname{Power}_{\max}}{\operatorname{T}_{\max} \cdot 2 \cdot \pi}$		
$\operatorname{max} = \operatorname{max} + \operatorname$						

### <u>Clutching - The Most Critical Element in Top Fuel Dragster Performance</u>

In drag racing, the clutch acts as the buffer between the power produced by the engine and the tires trying to apply it to the track surface. These cars, especially the fuel cars, are making so much power that it can't possibly be put to the ground all at once. There has to be something to take that power and apply it progressively through the RPM range or through the run, and allow the car to launch from a dead stop with a percentage of the engine's power then apply 100% of it when possible.

# IV. Macro Model of Motor Dynamics: Tire Velocity is v, ωk is RPM/1000

## Clutch, Tire, Down-Force Traction Model: Perfect Clutching - Constant Torque

Simple Step Model of Tire Traction (Assume perfect weight distribution, aerodynamics & wing design--> accleration ~ 4g) Tires do not have perfect grip, they may slip. Vehicle acceleration,  $a_{veh}$  is limited to the  $\mu$  = tire road force/vehicle weight tire traction (tire<sub>max\_g</sub>) ~ 4g. The tire rpm x GR = motor rpm, but because of slip, **initially**, tire velocity can be greater than vehicle velocity. When critical velocity is attained, the body and tire aerodynamics apply down force to increase  $\mu > 4$ .

**RPM x r<sub>tire</sub>/GR > v<sub>tire</sub> = v<sub>vehicle</sub>** <u>Case #1 Model Assumptions</u> <u>Perfect Clutching - Clutch Spin for max Torque.</u> Clutching to allow max motor torque to be applied to tires/road. Perfect Tire.

Acceleration initially jumps to max Torque, that is, to 4.3 g.

 $\frac{\text{RPM x r_{tire}}}{\text{GR}} = \frac{\text{V}_{tire}}{\text{W}_{tire}} = \frac{\text{V}_{tire}}{\text{W}_{tire}}$ 

<u>Case #2 Model Assumptions</u> <u>No Clutch or Tire Spin - Applied Torque & Power Follow the RPM Cun</u> Motor rpm has no slip to vehicle speed.

Acceleration rises, peaks at **4.3 g, and then falls**.

### Performance Model This model ignores various power losses and the boost in acceleration from aerodynamic down force

Angular Velocity Symbol, $\Omega$ (units of radians/second) $\Omega(\omega) := 2\pi 1000 \cdot \omega \cdot \min^{-1}$ RPM/1000 Symbol, $\omega_k$ RPM := $\min^{-1}$					
Angular Vel Ω @Max Power:	$\Omega_{\text{Pmax}} := \text{Power}_{\text{max}} \cdot \text{T}_{\text{max}}^{-1} \qquad \text{RPM}_{\text{Pmax}} := \frac{\Omega_{\text{Pmax}}}{2 \cdot \pi}$	$\text{RPM}_{\text{Pmax}} = 7245.38 \cdot \text{RPM}$			
Convert velocity to RPM	$VtoRPM(v_v) := v_v \cdot (1000 \cdot 2 \cdot \pi \cdot r_{tire} \cdot RPM)^{-1}$	$\omega_{\text{Pfall}} := \text{RPM}_{\text{Pmax}} \cdot \text{k}^{-1} = 7.25 \cdot \text{RPM}$			
Tire Velocity at Torque Fall:	$\mathbf{v}_{\mathrm{Tfall}} \coloneqq \mathrm{RPM}_{\mathrm{Pmax}} \cdot 2 \cdot \pi \cdot \mathbf{r}_{\mathrm{tire}} \cdot \mathrm{GR}^{-1}$	$v_{Tfall} = 269.44 \cdot mph$			
Tire Velocity to kRPM:	$VtokR(v_t) := v_t \cdot (k \cdot 2 \cdot \pi \cdot r_{tire} \cdot RPM)^{-1}$	$VtokR(60 \cdot mph) \cdot GR = 1.61$ $\theta := 0$			
Road Resistance, Ft:	$Ft(v_v) := M_{gross} \cdot g \cdot [T_{hys} \cdot v_v \cdot sin(\theta) + (RR_{tire} + RR_{road}) \cdot (RR_{tire} + RR$	$\cos(\theta) + \sin(\theta)$ RPM <sub>pmax</sub> for Max Power:			
Air Drag Force, Fa:	$Fa(v_{v}) := 0.5 \cdot \rho \cdot Ad \cdot \left[ \left( v_{v} + Vw \right)^{2} \cdot Cd + Cd_{cw} \cdot \left( V_{cw} \right)^{2} \right]$	<b><u>Note</u>:</b> For Drag and Road Resistance, approximate vehicle with v <sub>tire</sub> . At			
Total Opposing Force, Fo:	$Fo(v_v) := Fa(v_v) + Ft(v_v) \qquad Fo(60 \cdot mph) = 120.16 \cdot mph$	lbf <60mph Compared to Ftire, Fo is small.			
Torque/Force Falloff Curve:	$T_{PLt}(\omega_k) := Power_{max} \cdot \Omega(\omega_k)^{-1} \qquad T_m(\omega_k) := i$	$f\left(\omega_{k} \cdot RPM \geq \omega_{Pfall}, T_{PLt}(\omega_{k}), T_{max}\right)$			
Tm is Torque of motor		$\Gamma_{\rm m}(\omega_{\rm k})\cdot\mathbf{k}\cdot2\cdot\mathbf{\pi}\cdot\omega_{\rm k}\cdot\mathrm{RPM}$ $P_{\rm m}(8) = 8000\mathrm{hp}$			
Fmot, Tractive Force from motor, not from slipping tires:	$T_{mv}(v_t) := T_m(VtokR(v_t) \cdot GR) \qquad F_{mot}(v_t) :=$	$\frac{\text{GR}}{r_{\text{tire}}} \cdot T_{\text{mv}}(v_{\text{t}}) \qquad F_{\text{mot}}(1\text{mph}) = 1.11 \times 10^{4} \cdot \text{lbf}$			

# Solve for Velocity, Acceleration, and Distance versus Time

We are using Mathcad 14, a Computer Math Program, to do the Calculations: http://www.ptc.com/product/mathcad/free-trial

#### Case 1: Perfect Grip Tires at Maximum Motor Power, No limit on Coefficient of Tire Friction Newton's Third Law of Motion:

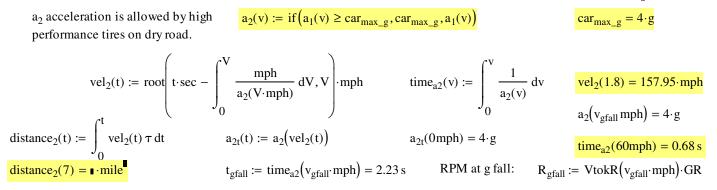
$$a_{1}(v) \coloneqq \frac{F_{mot}(v) - Fo(v)}{k_{m} \cdot M_{oross}} \qquad a_{1Tmax} \coloneqq \frac{T_{max} \cdot GR}{M_{gross} \cdot k_{m} \cdot r_{tire}} = 4.33 \cdot g$$

$$\bigvee_{w} \coloneqq 0 \cdot mph \qquad vel_{1}(t) \coloneqq root \left( t \cdot sec - \int_{0}^{V} \frac{mph}{a_{1}(V \cdot mph)} dV, V \right) \cdot mph \qquad time_{a1}(v) \coloneqq \int_{0}^{V} \frac{1}{a_{1}(v)} dv \qquad \frac{time_{a1}(74mph) = 0.78 \, s}{vel_{1}(3.83) = 327.44 \cdot mpl}$$

$$v_{gfall} \coloneqq root(a_{1}(V \cdot mph) - car_{max\_g}, V) = 196.06 \qquad time_{a1}(60mph) = 0.64 \, s \qquad a_{1t}(t) \coloneqq a_{1}(vel_{1}(t))$$

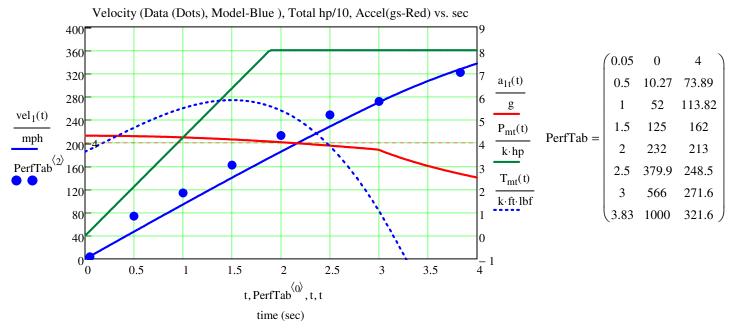
$$Velocity g fall, a \le 1.4g \qquad a_{1}(v_{gfall} mph) = 4 \cdot g \qquad a_{1t}(0) = 4.32 \cdot g$$

#### Case 2: High Performance 4 g Tires & Motor Drive Limited Accel < 4 g/ No Spin, but Max Power

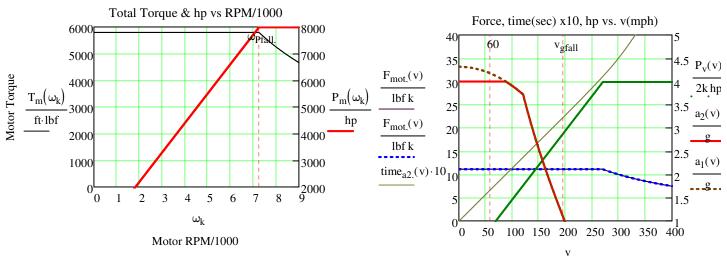


# V. Model Results and Validation: Matches Data

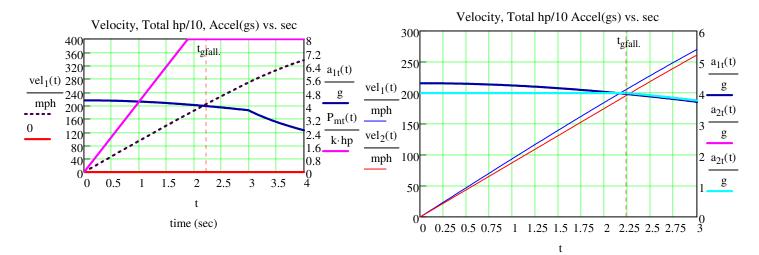
The difference between the data (dots) and Simulation Model is that the Model does not account for the aerodynamic down forces which give a boost in acceleration above 60 mph.



# **VI.** Performance Curves







time (sec)

# IX. Tire Friction (Composition and Width)

**Coefficient of Static Friction** ( $\mu$ ) is the ratio of Tire Road Force to Vehicle Weight. Values of  $\mu$  for Conventional Car tire On: Asphalt 0.72, Car tire Grass 0.35.

Top Fuel drag car tires are getting a coefficient of friction well over 4.5. How is this possible?

# This material came from:http://insideracingtechnology.com/tirebkexerpt1.htmSee Mathcad/EVs/Tire Friction.docRubber generates friction in three major ways:adhesion, deformation, and wear.

Rubber in contact with a <u>smooth surface</u> (glass is often used in testing) generates friction forces mainly by <u>adhesion</u>. When rubber is in contact with a <u>rough surface</u>, another mechanism, <u>deformation</u>, comes into play. Movement of a rubber slider on a rough surface results in the <u>deformation of the rubber by high points on</u> the surface called irregularities or <u>asperities</u>. A load on the rubber slider causes the asperities to <u>penetrate</u> the rubber and the rubber drapes over the asperities. The <u>energy needed</u> to move the asperities in the rubber comes from the <u>differential pressure</u> across the asperities as shown in Fig. 3.4, where a rubber slider moves on an irregular surface at speed V.



#### **Tearing and Wear**

As deformation forces and sliding speeds go up, local stress can exceed the tensile strength of the rubber, especially at an increase in local stress near the point of a sharp irregularity. High local stress can deform the internal structure of the rubber past the point of elastic recovery. When polymer bonds and crosslinks are stressed to failure the material <u>can't recover completely</u>, and this can cause <u>tearing</u>. Tearing absorbs energy, resulting in additional friction forces in the contact surface.

Wear is the ultimate result of tearing.

Ftotal = Fadhesive + Fdefformation + Fwear

### **Deformation Friction and Viscoelasticity**

Rubber is elastic and conforms to surface irregularities. But rubber is also viscoelastic; it doesn't rebound fully after deformation.

### **Hysteresis**

Hysteresis, or energy loss, in rubber.

where there is **some sliding** between the rubber and an irregular surface. If the **rubber recovers slowly** from the passing irregularity as in the high-hysteresis rubber, it **can't push on** the downstream surfaces of the irregularities **as hard** as it pushes on the upstream surfaces. This **pressure difference** between the **upstream and downstream faces of the irregularity** results in **friction forces** even when the surfaces are lubricated.

<u>Wide Tires:</u> It is true that wider tires commonly have better traction. The main reason why this is so does not relate to contact patch, however, but to **composition. Soft compound tires** are required to be **wider in order for the side-wall to support the weight** of the car softer tires have a larger coefficient of friction, therefore better traction. A narrow, soft tire would not be strong enough, nor would it last very long. Wear in a tire is related to contact patch. Harder compound tires wear much longer, and can be narrower. They do, however have a lower coefficient of friction, therefore less traction. Among tires of the same type and composition, here is no appreciable difference in 'traction' with different widths. Wider tires, assuming all other factors are equal, commonly have stiffer side-walls and experience less roll. This gives better cornering performance.

Friction is proportional to the normal force of the asphalt acting upon the car tires. This force is simply equal to the weight which is distributed to each tire when the car is on level ground. Force can be stated as Pressure X Area. For a wide tire, the area is large but the force per unit area is small and vice versa. The force of friction is therefore the same whether the tire is wide or not. However, asphalt is not a uniform surface. Even with steamrollers to flatten the asphalt, the surface is still somewhat irregular, especially over the with of a tire. Drag racers can therefore increase the probability or likelihood of making contact with the road by using a wider tir In addition a secondary benefit is that the wider tire increased the support base a

Friction force is independent of the apparent area of contact. For hard materials, this is nearly correct. The true area of contact varies with the applied load. The apparent area does not. If you can imagine the contact zone from a microscopic viewpoint, only a tiny portion of the apparent area actually touches. This tiny area is the true area of contact. But this applies to hard materials. It does not apply to elastomers, such as rubber. Tire tread rubber compounds vary greatly from one application to another. Race car tire tread compounds can be very soft, viscoelastic materials, while heavy truck tread rubber can be quite hard. In general, soft rubber materials have greater friction. With drag racing 'slicks,' the tire tread material literally sticks to the pavement--and the rubber is sheared from the tire. Clearly, the greater the apparent contact area, the greater this shear force. Cleanliness is important to getting the surfaces to 'stick.' This is one reason why drag racers have a 'burn-out' before each race (another is to raise the tire tread surface temperature). However, there is another reason for wide tire tread s on some road and track racing cars. They need tread volume to provide enough wear life. Tires wear rapidly under racing conditions. Some long races wear out several sets of tires. There are trade-offs with traction and tread life. That is why heavy truck tire tread compounds do not have as much friction as those used on passenger cars. However, truck tire tread compounds provide longer wear life and less heat build-up. Like many things in this world, tire tread choices involve compromises.